

Interdependence of Trade Policies in General Equilibrium

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Motivation

The Quantitative Revolution

- Explosion of quantitative gravity models featuring:
 1. Many differentiated (or homogeneous) sectors.
 2. Various *general equilibrium* interactions.

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- Gravity models have transformed the way economists think about international trade...
- ...but little impact on how we think about *trade policy!*

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 - Either purely computational...
 - ...or abstract from revenue-generating trade barriers (RTBs).
2. Many analysis of RTBs using the classical approach.
 - Assume homogeneous sectors.
 - Abstract from GE interactions.

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This Paper

- Adopt a GE multi-sector gravity model.
- Sectors are inter-related through:
 1. Factor price linkages.
 2. Cross price elasticity effects.

Goal 1: Solve for the optimal trade policy.

Goal 2: Characterize the interdependence of sector-level policies

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Main Findings

- GE environment \implies distinct tax structure:
 - Uniform tariffs + non-uniform export taxes
 - Key parameter: *sector-level trade elasticity*
- Policy interdependence:
 - Sector-level tariffs are complementary
 - Import policy *cannot* substitute export policy

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Theoretical Framework

The Environment

- K sectors
- Two countries: Home (h) and ROW (f)
- Perfect competition
- One “*Hicksian composite*” factor of production (L_i)

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- Y_i : total income
- $P_{i,k}$: price index of sector k in country i

Total welfare in country i

$$W_i = V_i(Y_i, P_{i,1}, \dots, P_{i,K})$$

- **Income effects:** $Q_{i,1}/Q_{i,2}$ can vary with Y_i
- **Cross-elasticity effects:** $Q_{i,1}$ responds to changes in $P_{i,2}$

CES import demand structure within sectors:

$$P_{i,k} = \sum_{j=h,f} A_{j,k} [\tau_{ji,k} (1 + t_{ji,k}) (1 + x_{ji,k}) w_j]^{-\theta_k}$$

- $A_{j,k}$: country j 's productivity level in sector k
- w_j : wage rate in country j
- θ_k : trade elasticity in sector k

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Three policy instruments:

- RTBs
 - Import tax by country i on country j exports: $t_{ji,k}$
 - Export tax by country j on own exports to country i : $x_{ji,k}$
- NRTBs
 - Iceberg or wasteful trade barriers: $\tau_{ji,k}$

Share of country i 's spending on country j varieties in sector k :

$$\lambda_{ji,k} = \frac{A_{j,k} [\tau_{ji,k} (1 + t_{ji,k}) (1 + x_{ji,k}) w_j]^{-\theta_k}}{\sum_{n=h,f} A_{n,k} [\tau_{ni,k} (1 + t_{ni,k}) (1 + x_{ni,k}) w_n]^{-\theta_k}}$$

Special case:

- $\theta_k \rightarrow \infty$: sectors are homogeneous.
- Ricardian model with K (possibly infinite) commodities.

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Total income in country i

$$Y_i = \text{factor income} + \text{IM tax rev.} + \text{EX tax rev.}$$

Trade and Income Levels

Total income in country i

$$Y_i = w_i L_i + \underbrace{\sum_k \frac{t_{ji,k}}{1 + t_{ji,k}} X_{ji,k}}_{\text{IM tax rev.}} + \underbrace{\sum_k x_{ij,k} X_{ij,k}}_{\text{EX tax rev.}}$$

- $X_{ji,k}$: **f.o.b.** value of exports from j to i
- $Y_{i,k}$ income spent on sector k

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- $X_{ji,k} = \frac{\lambda_{ji,k} Y_{i,k}}{1+t_{ji,k}}$
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Optimal Policy

Optimal Policy

- No foreign RTBs: $t_{hf,k} = x_{fh,k} = 0 \forall k$
- (For now) take the NRTBs as given.
- Solve for $\{x_k^*, t_k^*\}_k$
 - $t_k^* \equiv t_{fh,k}^*$ (Home's optimal tariff in sector k)
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Intermediate Step

- **Step 1:** assume $\{x_k\} = 0 \implies$ solve for $\{t_k^*\}$
- Social planners problem:

$$\max_{t_k} V_h(Y_h, P_h \mid \mathbf{x} = 0)$$

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Proposition 1: the optimal import tariff is uniform ($t_k^* = \bar{t}^* \forall k$):

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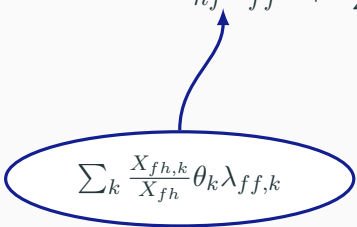
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wage effects

cross-elasticity
effects

Optimal Tariffs: *Special Cases*

- One sector economy (Gross 1987): $t^* = \frac{1}{\theta\lambda_{ff}}$
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- **Step 2:** jointly solve for \mathbf{x}^* and \mathbf{t}^*
- Social planner's problem

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Proposition 2: the optimal trade tax is composed of uniform tariff, t^* , and sector-specific export taxes such that:

$$(1 + t^*) (1 + x_k^*) = \frac{1}{\theta_k \lambda_{ff,k}}$$

- Unique *only* up to a uniform tariff, t^* .

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Optimal Tax Schedule

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- Optimal protection depends on:
 1. Sector-level trade elasticity, θ_k
 2. Sector-level comparative adv. (implicit in $\lambda_{ff,k}$)
special case

Optimal NRTBs

- **NRTBs:** non-revenue trade barriers or *iceberg trade costs*
- All policy instruments available \implies optimal policy includes

1. Zero NRTBs

$$\tau_{fh,k}^* = 0 \quad \forall k$$

2. Uniform tariffs + sector-specific export taxes:

$$(1 + t^*) (1 + x_k^*) = \frac{1}{\theta_k \lambda_{ff,k}}$$

- What if RTBs are unavailable?

Proposition 3: when RTBs are unavailable, the optimal NRTBs are *non-uniform* and *strictly positive* in sectors where θ_k is sufficiently large.

- Optimal U.S. NRTBs positive in *Wheat, Rice, Dairy,* and *Apparel* sectors.

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Policy Interdependence

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- **Proposition 4:** import tariffs are complementary: graph

$$t_1 \downarrow \implies t_2^*(t_1) \downarrow$$

- **Proposition 5:** import tariffs cannot substitute export taxes/subsidies

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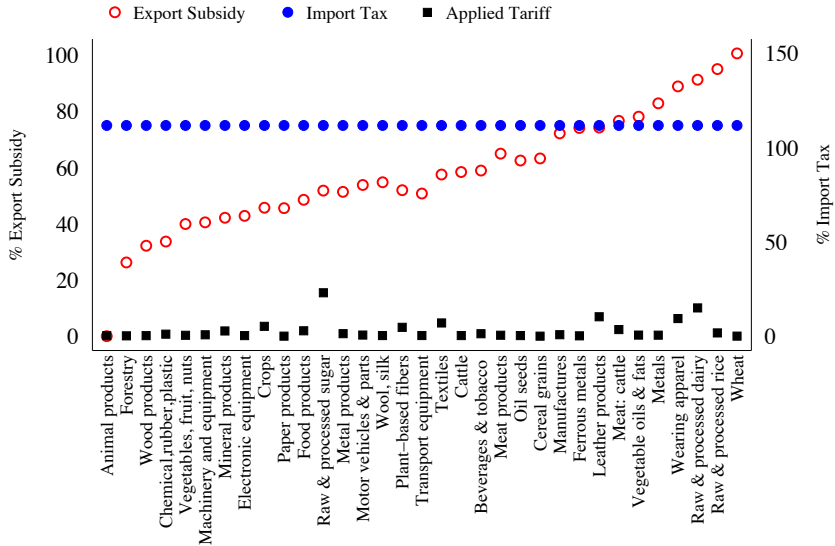
Quantitative Analysis

- We have established that GE effects matter, *theoretically*...
- ...but how important are GE effects, *quantitatively*?

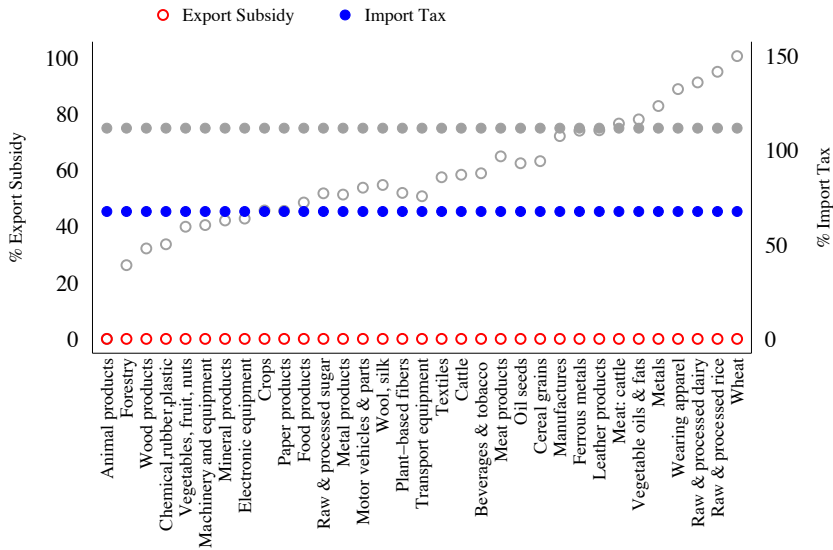
Calibrated Model

- Home: US
- Foreign: ROW
- 33 sectors
- θ_k 's from micro-level estimation.
- Match sector-level *production*, *trade*, and *expenditure* shares.

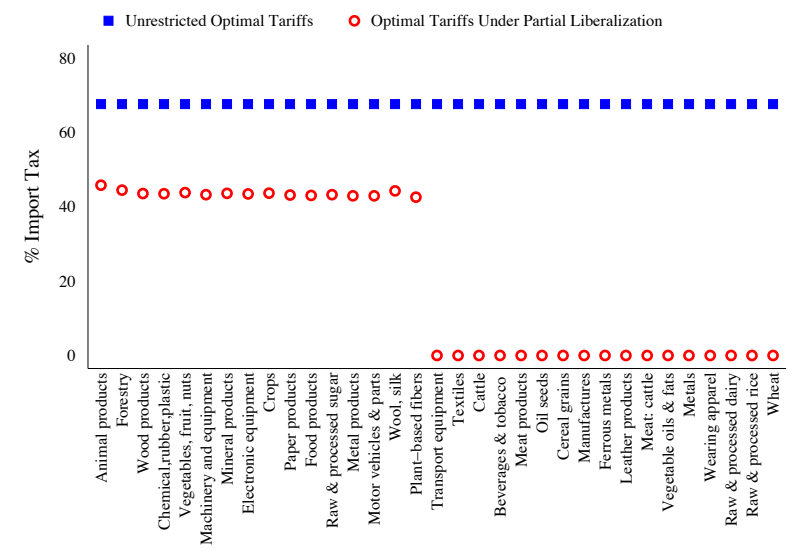
Unrestricted Optimal Tax Schedule



Optimal Tax Schedule when Export Policy is Restricted



Partial Liberalization



These policies have non-trivial welfare effects.

- **US:**
 - Optimal import policy \implies 3.48% welfare gains
 - Allow export policy \implies 0.07% higher gains
- **China:**
 - Optimal import policy \implies 2.26% welfare gains
 - Allow export policy \implies 0.20% higher gains

Concluding Remarks

- *Bottomline:* GE effects have important & non-trivial implications for trade policy.
- *Next step:* relax the linear cost assumption.
 - Marry the GE and traditional approaches.
 - Shed light on classical protectionist arguments (Graham 1923)

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- $\theta_k \rightarrow \infty \implies$ limit-pricing tax formula.
- Uniform tariff \bar{t}^* on import sectors.
- Tax on export sector:

$$(1 + \bar{t}^*) (1 + x_k^*) = \frac{\tilde{A}_{h,k}}{\tilde{A}_{f,k}} \tau_{hf,k} w$$

Return

Tariff Complementarity

